# Study of bulk and grain-boundary conductivity of $Ln_{2+x}Hf_{2-x}O_{7-\delta}$ (Ln = Sm-Gd; x = 0, 0.096) pyrochlores

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Received: 15 January 2008 / Accepted: 1 April 2009 / Published online: 9 May 2009 © Springer Science + Business Media, LLC 2009

Abstract The electrical conductivity of new solid electrolytes Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> have been compared with those for different pyrochlores including titanates and zirconates Ln<sub>2+x</sub>M<sub>2-x</sub>O<sub>7- $\delta$ </sub> (Ln = Sm-Lu; M = Ti, Zr; *x* = 0–0.81). Impedance spectroscopy data demonstrate that Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> synthesized from mechanically activated oxides have high ionic conductivity, comparable to that of their zirconate analogues. The bulk and grain-boundary components of conductivity in Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> (T<sub>synth</sub>=1600°C), Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> (T<sub>synth</sub>=1670°C) have been determined. The highest bulk conductivity is offered by the disordered pyrochlores prepared at 1600°C and 1670°C: ~1.5× 10<sup>-4</sup> S/cm for Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and 3×10<sup>-3</sup> S/cm for Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> at

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23952 Wismar, Germany 780°C, respectively. The conductivity of the fluorite-like phases at the phase boundaries of the  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Eu, Gd; M = Zr, Hf; *x*~0.286) solid solutions, as well as that of the high-temperature fluorite-like phases  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Eu, Gd; M = Zr, Hf; *x* = 0–0.286), is lower than the conductivity of the disordered pyrochlores  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Eu, Gd; M = Zr, Hf; *x*=0–0.096).

**Keywords** Pyrochlore · Fluorite · Total conductivity · Ionic conductivity · Mixed conductivity

### **1** Introduction

Mixed oxides possessing high oxygen ion conductivity typically undergo order-disorder (OD) phase transitions involving an increase in oxygen vacancy concentration. Studies of OD transitions on a microscopic scale from lattice defects to superstructure microdomains nucleating in the bulk of the parent phase are an effective approach to gaining insight into the mechanisms of ionic conduction in various oxides.  $Ln_2O_3$ -MO<sub>2</sub> (Ln = Sm-Gd; M = Zr, Hf) oxides are known to undergo a pyrochlore-fluorite OD phase transition [1, 2].

Oxygen ion conduction in the Ln<sub>2</sub>O<sub>3</sub>-HfO<sub>2</sub> (Ln = Nd, Sm-Gd) systems has been studied in less detail compared to the Ln<sub>2</sub>O<sub>3</sub>-ZrO<sub>2</sub> (Ln = Nd, Sm-Gd) systems. The reason for this is that Ln<sub>2±x</sub>Zr<sub>2±x</sub>O<sub>7±δ</sub> solid solutions are hightemperature oxygen ion conductors with significant compositional disorder and contain considerable concentrations of oxygen vacancies and/or interstitials [1–4]. Even though zirconium and hafnium differ very little in ionic radius (R Zr <sub>c.n. 6</sub><sup>4+</sup> = 0.72 Å; R Hf <sub>c.n. 6</sub><sup>4+</sup> = 0.71 Å), Hf-O bonds are more covalent than Zr-O because Hf has a filled 4f<sup>14</sup> shell, which ensures a more significant overlap of electron orbitals by virtue of its structure. As a result, the hafnates are less prone to defect formation and have significantly lower oxygen ion conductivity than do the zirconates [5]. The same is true for rare-earth stannates. Attempts to raise the ionic conductivity of  $Y_2Ti_2O_7$  via replacement of  $Ti^{4+}$ with the larger cation  $Sn^{4+}$ , intermediate in radius between  $Ti^{4+}$  and  $Zr^{4+}$ , for  $Y_2(Sn_yTi_{1-y})_2O_7$  series were unsuccessful in [6].  $Y_2Sn_2O_7$  remained fully ordered in the temperature range 25–1450°C. Clearly, in addition to the relationship between the radii of the A and B cations, the  $B^{4+}$ –O bond covalence is of importance. In particular, the  $Sn^{4+}$ –O bond in  $Y_2Sn_2O_7$  is far stronger than the  $B^{4+}$ –O bond in $Y_2(Zr_{0.6}Ti_{0.4})_2O_7$  [6]. The ionic conductivity in the  $Gd_2(Sn_yTi_{1-y})_2O_7$  system was also reported to drop for y>0.4, like that in the  $Y_2(Sn_yTi_{1-y})_2O_7$  system.

Interesting results were obtained by Moreno et al. [7], who used mechanically activated oxides in  $Gd_2(Sn_yZr_{1-y})_2O_7$ preparations. Moreno et al. [7, 8] obtained  $Gd_2(Sn_yZr_{1-y})_2O_7$ and  $Dy_2(Ti_{1-y}Zr_y)_2O_7$  by firing mechanically activated oxides at 1500°C for 36 h. Ionic conductivity measurements showed a jump in conductivity for y>0.4, similar to what was reported for  $Y_2(Zr_yTi_{1-y})_2O_7$  [6]. The  $Zr^{4+}$ –O bond in  $Gd_2(Sn_yZr_{1-y})_2O_7$  is far weaker than the  $Ti^{4+}$ –O bond in  $Gd_2(Sn_yTi_{1-y})_2O_7$ . Thus, those results provide further evidence that the reducing of the  $B^{4+}$ –O bond covalence is of importance for defect formation.

The first syntheses of  $Ln_{2+x}Hf_{2-x}O_{7-\delta}$  (x=0.096; Ln = Sm, Eu) and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> with the use of mechanical activation, which seems to favour the formation of antisite defects in cubic oxides, were reported in [9]. The materials were found to have high conductivity, approaching that of their zirconate analogues. The cation disorder in the hafnates, quantified by the density of  $Ln_{Hf} + Hf_{Ln}$ defects, was close to that in the zirconates [9]. The Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> solid solution has a pyrochlore-like structure over the entire temperature range studied, from 1000°C to 1670°C, whereas Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> undergo a transformation from a lowtemperature fluorite-like phase to a pyrochlore-like phase at 1200°C, accompanied by a rise in conductivity. Measurements in that study were performed only at a limited number of frequencies [9], so that the bulk and grainboundary components of conductivity could not be assessed separately. In this paper, we present a more detailed study of Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub>, Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub>. Samples synthesized at 1600°C or 1670°C were characterized by impedance spectroscopy with the aim of determining the bulk (intragranular) and grain-boundary components of conductivity.

The conductivity of new solid electrolytes Eu<sub>2.096</sub> Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> has been compared with conductivity of titanates and zirconates pyrochlores  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Sm–Lu; M = Ti, Zr; *x*=0–0.096).

#### 2 Experimental

 $Ln_{2.096}Hf_{1.904}O_{6.952}$  (Ln = Sm, Eu) and  $Gd_2Hf_2O_7$  were synthesized from  $Ln_2O_3$  and  $HfO_2$  powders mechanically activated in an eccentric vibratory mill with a 120 cm<sup>3</sup> vial volume [10]. The sample weight was 21 g, the ball-topowder weight ratio was ~15, and the vibration amplitude and frequency were 0.5 cm and 50 Hz.

In conductivity measurements, we used disc-shaped samples 10 mm in diameter and 2.5–3 mm in thickness, prepared by pressing the milled powders at 20–22 MPa, followed by heat treatment at 1200°C for 24 h, at 1600°C for 4 h or at 1670°C for 2 h.

Conductivity was determined by impedance spectroscopy (Zahner IM6E bridge) at frequencies from 0.01 Hz to 1 MHz. The measurements were made in the temperature range  $300-1000^{\circ}$ C at an oxygen pressure of  $10^{5}$ Pa. The same bridge was used to assess the electronic conductivity of the Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> sample synthesized at 1600°C. The resistance of the sample was measured at dc by the Hebb-Wagner method.

For some of the samples, we performed two-probe measurements in a NorECs ProboStat cell. The signal was monitored with a Beta-N impedance analyser at frequencies from 10 mHz to 3 MHz and temperatures from 400°C to 900°C. The applied voltage was 0.5 V, and the conductivity was determined to within 5% accuracy. Electrical contacts were made by applying ChemPure C3605 Pt paste followed by firing at 1000°C for 30 min.

The ceramics were characterized by x-ray diffraction (XRD) on a DRON-3M automatic diffractometer (Cu K  $_{\alpha}$ ;  $2\Theta$ =15–65°).

 $Sm_{2.096}Hf_{1.904}O_{6.952}$  was examined by electron diffraction on a JEOL JEM-2000FXII.

## **3** Results and discussion

The XRD patterns of the Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> samples prepared at 1200°C, 1600°C and 1670°C are shown in Fig. 1. Note, first of all, the presence of very weak pyrochlore superstructure peaks ((111), (311), (331) (almost indiscernible), (511)) and strong fluorite substructure peaks. Similar diffraction patterns were obtained earlier for Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> [9]. This type of XRD pattern, with weak superstructure peaks, was also reported for pyrochlore-like Ln<sub>2+x</sub>Zr<sub>2-x</sub>O<sub>7- $\delta$ </sub> in Ln<sub>2</sub>O<sub>3</sub>-ZrO<sub>2</sub> systems [11, 12]. The materials were assumed to have an anti-phase microdomain structure in a certain range of Ln<sub>2</sub>O<sub>3</sub> contents, resulting in a sharp drop in the intensity of the pyrochlore superstructure peaks. Deviations from stoichiometry in Gd<sub>2+x</sub>Zr<sub>2-x</sub>O<sub>7- $\delta$ </sub> were hypothesized to be compensated through the formation of anti-phase microdomain bound-



Fig. 1 XRD patterns of an  $Sm_2O_3 + 2$  HfO<sub>2</sub> mixture mechanically activated at 25°C (1) and  $Sm_{2.096}$ Hf<sub>1.904</sub>O<sub>6.952</sub> samples heat-treated at 1000°C (2), 1200°C (3), 1300°C (4), 1450°C (5), 1600°C (6) and 1670°C (7)

aries [13]. The coordination number of the Gd cations near the anti-phase boundaries was assumed to be below 8, in contrast to the octahedral coordination of lanthanides in the pyrochlore structure [13]. Last investigations of titanates  $Ln_2TiO_5$  (pyrochlore structure) show that the low intensity of the pyrochlore superstructure reflections is due to the small size of pyrochlore microdomains embedded in fluorite matrix [14]. The possibility of the observation of that microdomain stucture by electron microscopy often has limited by technical level of the electron microscope type.

Figure 2(a) shows the 300°C and 400°C impedance spectra of the Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> sample synthesized at 1600°C. In the inset of Fig. 2(a), one can clearly see two semicircles, corresponding to the bulk (high frequencies) and grain-boundary (medium frequencies) components of conductivity, and the portion representing conduction across the sample-electrode interface. Clearly, at these low temperatures, the conductivity is determined by the grainboundary component. With increasing temperature, however, the grain-boundary component of resistance decreases considerably more rapidly than the bulk component. Figure 2(b) shows the 600°C impedance spectra of the Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> samples synthesized at 1200°C, 1600°C and 1670°C. In the three spectra, the high- to medium-frequency arc is a combination of the semicircles due to the bulk (intragranular) and grain-boundary components of conductivity. The low-frequency arc represents charge transport across the electrode-sample interface. In contrast to the low-temperature spectra, the 600°C grainboundary and bulk charge transport processes are very close in parameters, as evidenced by the significant overlap of the semicircles representing these processes. In the three spectra, the significant overlap of the bulk and grain-boundary components of conductivity makes it difficult to separately evaluate them. At higher temperatures, this is impossible. Electronic conductivity of the  $Sm_{2.096}Hf_{1.904}O_{6.952}$  assessed by Hebb-Wagner technique was at least three orders of magnitude lower then the ionic component.

Figure 3(a) presents the Arrhenius plots of the bulk and grain-boundary components of conductivity for the Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> prepared at 1600°C. Note that the activation energy for bulk conduction is as low as 0.55 eV, whereas that for grain-boundary conduction is 0.97 eV. This low activation energy for bulk conduction is atypical of oxygen ion conductors. However, for pyrochlores, this is not so special. Further lower activation energy of 0.51 eV was reported in [15]. Figure 3(b, c) shows the Arrhenius plots of bulk and grain-boundary conductivities for the Eu<sub>2 096</sub>Hf<sub>1 904</sub>O<sub>6 952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> samples synthesized at 1670°C. The impedance spectroscopy data demonstrate that these samples have high conductivities:  $5 \times 10^{-3}$  µ  $3 \times$  $10^{-3}$  S/cm, respectively, at 780°C. The bulk conductivity of  $Eu_{2.096}Hf_{1.904}O_{6.952}$  is notably higher than its grain-boundary conductivity over the entire temperature range studied, up to 1000°C. So the bulk conductivity of  $\text{Sm}_{2.096}\text{Hf}_{1.904}\text{O}_{6.952}$  is lower the conductivity of Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> samples. The data [9], obtained only at a limited number of frequencies, were confirmed by impedance spectroscopy data in this investigation.

Grain size and density data for the materials studied are presented at Fig. 4. The average grain size of the  $Ln_{2.096}Hf_{1.904}O_{6.952}$  (Ln = Sm, Eu) samples is  $1-2\mu$ m as determined by SEM. Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> consists of both coarse (3–4µm) and fine ( $\approx 200$  nm) grains. The relative densities of Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> reach 95.5% and 97.8%, respectively; that of Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> is slightly lower, 92.3%. SEM data correlate with the above relationship between the bulk and grain boundary conductivities of our samples. The large grain size of Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> leads to a higher grain boundary conductivity, whereas in Ln<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> (Ln = Sm, Eu) the bulk conductivity exceeds the grain boundary conductivity.

Figure 5(a) shows the total conductivity for  $Gd_2Hf_2O_7$ , Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> samples obtained at 1200°C, 1600°C and 1670°C according [9]. Figure 5(b) shows the anti-structure pairs Ln<sub>Hf</sub> + Hf<sub>Ln</sub> and Ln<sub>Hf</sub> defects number for samples synthesized at 1600°C. Best ion-conducting samples Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub>, Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> have 8–16% anti-structure pairs Ln<sub>Hf</sub> + Hf<sub>Ln</sub> at the room temperature. Sm<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> obtained at 1600°C and 1670°C didn't show anti-structure pairs Sm<sub>Hf</sub> + Hf<sub>Sm</sub> and its Fig. 2 (a) 300°C and 400°C impedance spectra of the  $Sm_{2.096}Hf_{1.904}O_{6.952}$  sample synthesized at 1600°C and (b) 600°C impedance spectra of the  $Sm_{2.096}Hf_{1.904}O_{6.952}$  samples synthesized at 1200°C, 1600°C and 1670°C



total conductivity is one order magnitude lower then that of  $Gd_2Hf_2O_7$ . The results [16] showed that  $Ln_{Ti}^{'}$  and  $Ti_{Ln}^{\bullet}$  defects form easily in rare-earth titanates in the heating process and often disappear in the cooling process. We have another situation for  $Gd_2Hf_2O_7$ ,  $Eu_{2.096}Hf_{1.904}O_{6.952}$  in this work.  $Ln_{Hf}^{'}$  and  $Hf_{Ln}^{\bullet}$  defects induced by mechanical activation with subsequent sintering at high temperature 1600–1670°C in hafnates were preserved during the cooling down to the room temperature.

In this context, it should be discussed the mechanical activation and its role in the generation of anti-site defects in the pyrochlore structure. The high-conductivity DP phase of the  $Ln_2Ti_2O_{7-\delta}$  titanates contains  $Ln'_{Ti} + Ti^{\bullet}_{Ln}$  anti-structure pairs and oxygen vacancies in the temperature range of our conductivity measurements (450–950°C). These defects may relax during cooling or storage if the

samples were synthesized using co-precipitation [17]. Similar results were reported by Eberman et al. [16] for  $(Sc_{z}Yb_{1-z})_{2}Ti_{2}O_{7}$ . However, in the synthesis of titanates with the use of mechanical activation followed by firing,  $Ln'_{Ti} + Ti_{Ln}^{\bullet}$  cation defects may be stabilized, as was found for Yb2Ti2O7, which was shown to contain about 4.5%  $Yb'_{Ti} + Ti^{\bullet}_{Yb}$  anti-structure pairs at room temperature [17]. In the  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Sm–Gd; M = Zr, Hf; x=0-0.286) systems, anti-structure pairs (5-22%) were found at room temperature in  $Ln_2M_2O_7$  (M = Zr, Hf) samples synthesized using mechanical activation [9]. The relaxation of anti-site defects in the Ln2Ti2O7 titanates during cooling or room-temperature storage and their stability in the  $Ln_2M_2O_7$  (M = Zr, Hf) materials suggest that anti-structure pairs are more stable at a smaller difference in ionic radius between Ln<sup>3+</sup> and M<sup>4+</sup>. In



Fig. 3 (a) Arrhenius plots of the bulk and grain-boundary components of conductivity for the  $Sm_{2.096}Hf_{1.904}O_{6.952}$  sample synthesized at 1600°C, (b) Arrhenius plots of bulk and grain-boundary conductivities for the  $Eu_{2.096}Hf_{1.904}O_{6.952}$  and (c)  $Gd_2Hf_2O_7$  samples synthesized at 1670°C

particular, the difference is 0.38Å (the largest) in the titanates, 0.346Å in the zirconates and 0.343Å in the hafnates. In a recent paper, Fuentes et al. [18] have described the synthesis of lanthanide titanate pyro-

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chlores through mechanical processing in a planetary mill, which demonstrates that mechanochemical synthesis of pyrochlores does occur at room temperature. Thus, both anti-site defects and oxygen vacancies can be produced by mechanical processing. Clearly, subse-



Fig. 4 SEM pictures for  $\rm Sm_{2.096}Hf_{1.904}O_{6.952}$  1600°C (a),  $\rm Eu_{2.096}Hf_{1.904}O_{6.952}$  1670°C (b),  $\rm Gd_2Hf_2O_7$  1670°C (c)



Fig. 5 Total conductivity (a) and  $Ln_{\rm Hf}$  +  $Hf_{Ln}$  anti-structure pairs and  $Ln_{\rm Hf}$  defects (b) for  $Sm_{2.096}Hf_{1.904}O_{6.952}$ ,  $Eu_{2.096}Hf_{1.904}O_{6.952}$  and  $Gd_2Hf_2O_7$  samples synthesized at 1600°C

quent high-temperature heat treatment influences the defect structure of the titanates. At the same time, the fact that defects (4.5%) were found in Yb<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> at room temperature after high-temperature synthesis from a mechanically activated mixture [17] suggests that mechanical activation may produce defects in appropriate symmetrical structures and that some of the defects may persist after high-temperature annealing. Since the M<sup>4+</sup>–O bonds in the hafnates and zirconates are less covalent than those in the titanates [19], mechanical activation of Ln<sub>2</sub>M<sub>2</sub>O<sub>7</sub> (Ln = Sm – Gd; M = Zr, Hf) is also quite likely to produce anti-site defects.

As it was stated before, among the  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Sm-Gd; M = Zr, Hf) solid solutions lying in the homogeneity range of the pyrochlore phases  $Ln_2M_2O_7$  (M = Zr, Hf), the highest conductivity is offered by nominally stoichiometric compounds with a distorted pyrochlore structure (this phase has  $Ln_{Hf}$  and  $Hf_{Ln}$  defects) and by pyrochlore-like solid solutions with small deviations from stoichiometry [2, 9].

Clearly, the high-temperature phases of  $Ln_2M_2O_7$  (Ln = Sm-Gd; M = Zr, Hf) have the optimal concentration and

mobility of oxygen vacancies, which are generated according to the schemes:

$$Ln_{Ln}^{\ x} + M_{M}^{\ x} \to Ln_{M}^{\ \prime} + M_{Ln}^{\bullet}$$
<sup>(1)</sup>

$$O_0{}^x \to V_{O(48f)}{}^{\bullet\bullet} + O_{i(8b)}{}^{''}$$

$$\tag{2}$$

The excess  $Ln^{3^+}$  ions in  $Ln_{2^+x}M_{2^-x}O_{7^-\delta}$  (Ln = Sm–Gd; M = Zr, Hf) are presumably accommodated in the  $M^{4^+}$  site; i.e., the general formula can be written in the form  $Ln_2$   $(M_{2^-x}Ln_x)O_{7^-\delta}$ . Residing in the B site of the pyrochlore  $(A_2B_2O_7)$  structure,  $Ln^{3^+}$  favors the formation of oxygen vacancies according to the scheme:

$$Ln_2O_{3\to MO2} \to 2(Ln_M)' + V_{O(48f)}^{\bullet\bullet} + 3O_O^x$$
 (3)

The oxygen vacancy concentration must, therefore, increase with x.

However, like in the  $Ln_{2+x}Ti_{2-x}O_{7-x/2}$  (Ln = Er–Lu) solid solutions, the conductivity was found to decrease with increasing Ln content. This is, most likely, due to Ln – vacancy association according to the scheme:

$$Ln_{M}' + V_{O}^{\bullet \bullet} \leftrightarrow (Ln_{M}V_{O})^{\bullet}$$

$$\tag{4}$$

High Ln contents lead to the formation of defect clusters, which contain both cation anti-structure pairs and anion pairs (Frenkel defects):

$$Ln_{Ln}{}^{x} + M_{M}{}^{x} + O_{o}{}^{x} \rightarrow \left\{ Ln_{M}{}^{'} + M_{Ln}{}^{\bullet} + V_{O(48f)}{}^{\bullet\bullet} + O_{i(8b)}{}^{''} \right\}^{x}$$
(5)

It seems likely that the reduction in ionic conductivity with increasing Ln content is due to a decrease in carrier mobility rather than to a decrease in carrier concentration. The conductivity of heavily doped fluorite-like phases at the pyrochlore-fluorite phase boundary, as well as that of the high-temperature fluorite-like phases  $Ln_2M_2O_7$  (M = Zr, Hf), is always lower than the conductivity of the distorted pyrochlores and pyrochlore-like solid solutions.

The same results follow from the data reported by van Dijk et al. [2]. In that work, a single crystal of composition  $Gd_{0.52}Zr_{0.48}O_{1.74}$ , lying in the pyrochlore-like solidsolution region, with an excess of  $Gd_2O_3$ , was quenched from the synthesis temperature (~2500°C) and then annealed for 20 h at 1250°C, i.e., well below 1530°C, the temperature of the pyrochlore-fluorite OD phase transition (sample A). Sample A and a sample of the same composition (B) quenched from the synthesis temperature (2500°C) were characterized by XRD. Pyrochlore superstructure peaks were only detected in the XRD pattern of sample A, while that of sample B showed only fluorite substructure peaks. Conductivity measurements showed



Fig. 6 Ionic conductivity (*filled data points*) and activation energy (*open data points*) as functions of the radius of the lanthanide for  $Ln_2M_2O_7$  (Ln = Sm-Lu; M = Ti, Zr, Hf)

that the pyrochlore-structured crystal (sample A) had a higher bulk conductivity and lower activation energy in comparison with sample B. In later studies of the hightemperature OD transition in polycrystalline  $Gd_2Zr_2O_7$ ( $T_{OD}$ =1530°C) [12], the fluorite-like phase quenched from 1700°C, i.e., from above the transition temperature, contained pyrochlore microdomains and was, in fact, a heavily disordered pyrochlore rather than a pure fluorite. That material had a lower bulk conductivity in comparison with the material synthesized at 1550°C, which had a slightly distorted pyrochlore structure.

Present investigation shows that the new solid electrolytes  $Gd_2Hf_2O_7$  and  $Eu_{2.096}Hf_{1.904}O_{6.952}$  can be included in the high temperature conducting pyrochlores  $Ln_{2+x}M_{2-x}O_{7-x/2}$  (Ln = Sm–Lu; M = Ti, Zr, Hf) family.

At least we would like to discusse the temperature effect on conductivity of the pyrochlore-like  $Ln_{2+x}M_{2-x}O_{7-x/2}$  (Ln = Sm-Lu; M = Ti, Zr, Hf).

Raising the temperature influences:

- (1) the generation of anti-site defects and oxygen vacancies,
- (2) oxide ion mobility,
- (3) metal-oxygen  $(M^{4+}-O)$  bond covalency.

The cation radius difference,  $\Delta R$ , influences the generation of anti-site defects and oxygen vacancies: the smaller the difference, the higher the probability of the formation of anti-structure pairs and oxygen vacancies. With increasing temperature, the concentration of anti-structure pairs increases.

The  $M^{4+}$ -O bond covalency decreases in the order  $Sn^{4+}$ -O >  $Ti^{4+}$ -O >  $Hf^{4+}$ -O >  $Zr^{4+}$ -O [19]. This implies that the  $Zr^{4+}$ -O bond has the greatest tendency to break, leading to defect formation in the pyrochlore structure.

With increasing temperature, the tendency for  $M^{4+}$ –O bonds to break becomes more pronounced in the same order.

Our results (Figs. 6, 7) demonstrate that, among the  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Sm – Lu; M = Ti, Zr, Hf; x=0-0.81) materials studied, the highest conductivity is offered by  $Yb_2Ti_2O_7$  and  $Yb_{2+x}Ti_{2-x}O_{7-\delta}$  (x=0.096) solid solution as well as  $Eu_{2.096}Hf_{1.904}O_{6.952}$  and  $Gd_{2.096}Zr_{1.904}O_{6.952}$ . At the same time, the cation radius difference in Yb<sub>2</sub>Ti<sub>2</sub>O<sub>7</sub> (0.38 Å) is greater than that in the high-conductivity  $Eu_2M_2O_7$ with M = Zr and Hf (0.346Å in the zirconates and 0.356 Å in the hafnates), and the Ti<sup>4+</sup>-O bond covalency is the highest among the M<sup>4+</sup>–O bonds in  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (M = Ti, Zr, Hf). Our measurements were performed in the range 300-1000°C. Thus, with increasing temperature the highest conductivity is offered by compounds in which  $\Delta R$  and bond covalency are far from being the lowest. The relationship seems to be more complex. We believe that the small cation size is also essential.

## 4 Conclusions

The electrical conductivity of pyrochlore-like  $Ln_{2.096}$ Hf<sub>1.904</sub>O<sub>6.952</sub> (Ln = Sm, Eu) solid solutions and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> synthesized in the range 1600–1670°C using mechanical activation was determined for the first time by impedance spectroscopy. Eu<sub>2.096</sub>Hf<sub>1.904</sub>O<sub>6.952</sub> and Gd<sub>2</sub>Hf<sub>2</sub>O<sub>7</sub> pyrochlores are shown to have high ionic conductivity according to its energy activation (0.85 eV and 0.62 eV, respectively), comparable to that of their zirconate analogues. The highest conductivity is offered by pyrochlores slightly disordered in both the anion and cation sublattices. The conductivity of the high-temperature fluorite-like



Fig. 7 Ionic conductivity (*filled data points*) and activation energy (*open data points*) as functions of the radius of the lanthanide for  $Ln_{2.096}Hf_{1.904}O_{6.952}$  (Ln = Sm-Lu; M = Ti, Zr, Hf)

phases  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (M = Zr, Hf), as well as that of heavily doped fluorite-like phases at the phase boundary of  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (M = Zr, Hf), is always lower than the conductivity of the disordered pyrochlores.

Some factors, which may effect on the oxide ion conductivity of pyrochlore-like  $Ln_{2+x}M_{2-x}O_{7-\delta}$  (Ln = Sm–Lu; M = Ti, Zr, Hf; M = 0–0.81) are discussed.

Acknowledgements This work was supported by the Presidium of the Russian Academy of Sciences (program "Synthesis of Inorganic Substances with Controlled Properties and Fabrication of Related Functional Materials," grant no. 18P/2009), the Russian Foundation for Basic Research (grant no. 07-03-00716), the Department of Materials Sciences of the Russian Academy of Sciences (program of the Basic Investigations of New Metal, Ceramic, Glass- and Composite-Materials and the Deutsche Forschungsgemeinschaft (grant no. CZ 436RUS17/96/06).

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